



MODIFIED DIJKSTRA ALGORITHM FOR DETERMINING MULTIPLE SOURCE SHORTEST PATH OF HOSPITAL LOCATION IN RIVERS STATE (NIGERIA)

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Abstract

Determining the shortest path (road network) to a particular hospital in the case of emergency could determine patient survival or not. The approach currently on ground in Rivers State, Nigeria is subjective (depending on the skill, experience and exposure of the personnel prescribing the distance and not based on an objective approach) at best. This research paper, has adapted Dijkstra algorithm base on it drawback to propose a modified Dijkstra algorithm capable of implementing multiple source shortest path distance optimization to varied hospital within Rivers State. Matrix Laboratory (MatLab) and Hypertext preprocessor (PHP) were the simulation tools and language of implementation respectively. The results of our simulation were satisfactory having been able to implement Multiple Source Shortest Path across several hospitals spread across Rivers State.

Introduction

River State, Nigeria is a commercial, multi-culture and age range city, with population density (persons with various attributes; age person, younger person, nursing mothers etc.) on the steady increase resulting in increased road creation, industries, residential estates as well creating chaotic and hectic traffic jam (CAPD, 2014). The health of every individual is of paramount importance to himself and the country of origin. It is important that securities of lives are guaranteed through quick response to health issues when they occur. The conventional approach adopted for distance optimization to a given health or medical center and hospital from a given community within Rivers State has been subjective at best; depending on the will, emotional state and experiences of an individual expert prescribing such information utilizing his/her head knowledge (Osami, 2013). There continuous and rapid optimization are totally impossible. This approach though useful in the age of no computer or computational devices has proving obsolete with the passage of time where most, if not all human endeavors are based on computer approaches. The loss of life, or even irreplaceable damages incurred by a patient due to poor distance prescription (delay time) to a given hospital has indeed been enormous within Rivers State. This research paper is geared toward proposing an implementing a Modified Dijkstra Algorithm for Determining Multiple Source Shortest Path of Hospital Location in Rivers State (Nigeria).

Review of related literature

Pi6ro et al. (2002), handled flow allocation problems in IP networks using open shortest path first (OSPF) routing. Their main purpose was to discuss and propose methods for finding settlements of OSPF link weight system realizing the assumed demand pattern for the given network resources (links capacities). They discovered that such settlements can result in a significantly better network performance compared with the simplified weight setting heuristics typically used nowadays. Although the configuration of the link weight system is primarily done in the network planning phase, additional re-optimizations are feasible, and in fact essential, in order to cope with major changes in traffic conditions and with major resources' failures and rearrangements. Their work formulates a relevant OSPF routing optimization problem, proves it's NP-completeness, and discusses possible heuristic approaches and related optimization methods for solving it. Two basic approaches were considered (the direct approach and the two-phase approach) and the resulting optimization algorithms are presented. Their considerations, finding and results were illustrated with numerical results.

John and Patrick (2004) applied the meta-heuristic method of ant colony optimization (ACO) to solve set of vehicle routing problems (VRP). Their procedure simulates the decision-making processes of ant colonies as they forage for food and is similar to other adaptive learning and artificial intelligence techniques. Modifications were made to the ACO algorithm used to solve the traditional traveling salesman problem in order to allow the search of the multiple routes of the VRP. Experimentation shows that their algorithms were successful in finding solutions within 1% of known optimal solutions and the use of multiple ant colonies is found to provide a comparatively competitive solution technique especially for larger problems. Additionally, the size of the candidate lists used within the algorithm is a significant factor in finding improved solutions, and the computational times for the algorithm compare favorably with other solution methods.

Xing (2011), handled the Capacitated Arc Routing Problem (CARP) which is representative of numerous practical applications, and in order to widen its scope, they consider an extended version of this problem that entails both total service time and fixed investment costs. We subsequently propose a hybrid ant colony optimization (ACO) algorithm (HACOA) to solve instances of the



extended CARP. Their approach was characterized by the exploitation of heuristic information, adaptive parameters, and local optimization techniques: Two kinds of heuristic information, arc cluster information and arc priority information are obtained continuously from the solutions sampled to guide the subsequent optimization process. The adaptive parameters ease the burden of choosing initial values and facilitate improved and more robust results. Finally, local optimization, based on the two-opt heuristic, is employed to improve the overall performance of the proposed algorithm. The resulting HACO is tested on four sets of benchmark problems containing a total of 87 instances with up to 140 nodes and 380 arcs. In order to evaluate the effectiveness of their proposed method, some existing capacitated arc routing heuristics are extended to cope with the extended version of this problem; the experimental results indicate that the proposed ACO method outperforms these heuristics.

In optimization of a design, the design objective could be simply to minimize the cost of production or to maximize the efficiency of production. An optimization algorithm is a procedure which is executed iteratively by comparing various solutions still an optimum or a satisfactory solution is found. With the advent of computers, optimization has become a part of computer-aided design activities (Jason, 2011).

Mathematically, optimization is defined as the search for combination of parameters commonly referred to as decision or design variables ($X=[X_1, X_2, X_3 \dots X_n]$) which minimize or maximize some ordinal quantity (C) (typically a scalar called a score) assigned by an objectives function or cost function (F), under a set of constraints ($g=[g_1, g_2, g_3 \dots g_n]$). For example, a general minimization case would be as follows: $f(x_1) \leq f(x)$, for all x_i belonging to x (Jason, 2011). The following are ingredient under optimization:

Decision variables: The formulation of an optimization problem begins with identifying the underlying design variables, which are primarily varied during the optimization process (Kennerley, 2012). A design problem usually involves many design parameters, of which some are highly sensitive to the proper working of the design. These parameters are called design variables in the parlance of optimization procedures. Other design parameters usually remain fixed or vary in relation to the design variables (Michael, 1999 and Malcolm, 2006). The first thumb rule of the formulation of an optimization problem is to choose as few design variables as possible (Kennerley, 2012). The outcome of that optimization procedure may indicate whether to include more design variables in a revised formulation or to replace some previously considered design variables with new design variables (Kennerley, 2012).

Objective functions: The next task in the formulation procedure is to find the objective function in terms of the design variables and other problem parameters. The common engineering objectives involve minimization of overall cost of manufacturing or minimization of overall weight of a component or maximization of total life of a product or others. Be possible to formulate mathematically (Leader, 2010).

Constraints: The constraints represent some functional relationships among the design variables and other design parameters satisfying certain physical phenomenon and certain resource limitations (Wenyu and Ya-Xiang, 2010). The nature and number of constraints to be included in the formulation depend on the user. Constraints may have exact mathematical expressions or not. For example, maximum stress is a constraint of a structure (Dechter, 2003). If a structure has regular shape they have an exact mathematical relation of maximum stress with dimensions. But incase irregular shape, finite element simulation software may be necessary to compute the maximum stress (Leader, 2010)

Methodology of the research

Dijkstra Algorithm is one of the predominantly shortest routing solutions to shortest path problem which is showed in figure 3.1

1. function Dijkstra (Graph, source);
2. for each vertex v in Graph: // Initializations
3. $\text{dist}[v] := \text{infinity}$; // Unknown distance function from
4. // source to v
5. $\text{previous}[v] := \text{undefined}$; // Previous node in optimal path
6. end for // from source
- 7.
8. $\text{dist}[\text{source}] := 0$; // Distance from source to source
9. $Q := \text{the set of all nodes in Graph}$; // All nodes in the graph are
10. // unoptimized – thus are in Q
11. while Q is not empty: // The main loop
12. $u := \text{vertex in } Q \text{ with smallest distance in } \text{dist} []$; // Source node in first case
13. remove u from Q ;



```

14. if dist[u] = infinity:
15. break ;                      // all remaining vertices are
16. end if                      // inaccessible from source
17.
18. for each neighbor v of u:    // where v has not yet been
19.                             // removed from Q.
20. alt := dist[u] + dist_between(u, v) ;
21. if alt < dist[v]:           // Relax (u,v,a)
22. dist[v] := alt ;
23. previous[v] := u ;
24. decrease-key v in Q;       // Reorder v in the Queue
25. end if
26. end for
27. end while
28. return dist;
29. end function

```

Figure 3.1: Dijkstra Algorithm (Melissa, 2012)

Dijkstra Algorithm propagates one major demerit which fosters this research paper. Dijkstra Algorithm supports the Single Source Shortest Path; which imply that for any routing problem we must have one source vertex and a single destination or multiple destination path.

The proposed modified dijkstra algorithm for determining multiple source shortest path of hospital location

The proposed Algorithm extends the scope and focus of the current algorithm, there providing a framework in which multiple source vertexes are possible. This Algorithm will be inappropriate in solving multiple source vertex problems which is indeed the bedrock of most real world problem, but still date few of these algorithm has be proposed for handling the aforementioned problem. The algorithm is depicted on Figure 3.2

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1. Function Dijkstra // Graph, Source-Vertices
2. For each Vertex (V) in the Graph (G) ∉ Source -Vertices (SV); // V: = Hospitals in River State, SV: = Communities,
   Towns or Junctions all in River State
3. Dist [V] := ∞; // Unknown distance for all non- source vertices in the graph
4.
5. Previous [V] := Undefined;
6. End for
7.
8. Dist [SV1] := 0 // No previous nodes with optimal path form SV1
9. M1: = First Queue holding the set of all nodes (V) in the Graph (G) ∉ Source-Vertices 1 (SV1)
10. While M1 ≠ empty:
11. Y1:= Vertices in M1 with Shortest distance in Dist [V];
12.
13. Remove Y1 from M1;
14. If Dist[Y1]: = ∞ // Unknown distance from neighboring nodes of Y1 in the Graph;
15. Break;
16. End if;
17. For each neighboring V of Y1 with Dist [V1,V2,V3... Vn]
18. K1:=neighboring Vertices (V) of Y1
19. K1:= Dist [SV1,Y1] + Dist [Y1,K1]
20. If K1[Dist]< Dist[V1,V2,V3... Vn]
21. Remove K1 from M and add to SV1, Y1
22. Decrease-Key Y1 in M1
23. While M1 = empty
24. Endif

```



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25. End For
26. End while
27. While M2 ≠ empty:
28. Y2:= Vertices in M1 with Shortest distance in Dist [V];
29.
30. Remove Y2 from M2;
31. If Dist[Y2]: = ∞ // Unknown distance from neighboring nodes of Y2 in the Graph;
32. Break;
33. End if;
34. For each neighboring V of Y2 with Dist [V1,V2,V3...Vn]
35. K2:=neighboring Vertices (V) of Y2
36. K2:= Dist [SV2,Y2] + Dist [Y2, K2]
37. If K2 [Dist]< Dist[V1,V2,V3...Vn]
38. Remove K2 from M and add to SV2, Y2
39. Decrease-Key Y2 in M2
40. While M2 = empty
41. Endif
42. End For
43. End While
44. End

```

Figure 3.2: The Proposed Modified Dijkstra Algorithm

Implementation and simulation

The implementation of the modified algorithm was handled utilizing Matrix Laboratory (MATLAB) which serves as our simulation tool in testing the algorithm interactively. It's also provided an interactive environment for algorithm development, data visualization, data analysis, and numerical approach which was relevant to our numerical dataset which was more appropriate than with spreadsheets or traditional programming languages, such as C/C++ or Java. After pruning the dataset utilizing MATLAB, the algorithm was fully implemented utilizing Hypertext Preprocessor (PHP), which served as the language of implementation.

Simulation results (application of the modified dijkstra algorithm)

The graph network on Figure 3.3 shows the application of Dijkstra algorithm and the Modified approach adopted. The full application of the modified application fosters multiple source path as opposed the single source path generated by Dijkstra Algorithm.

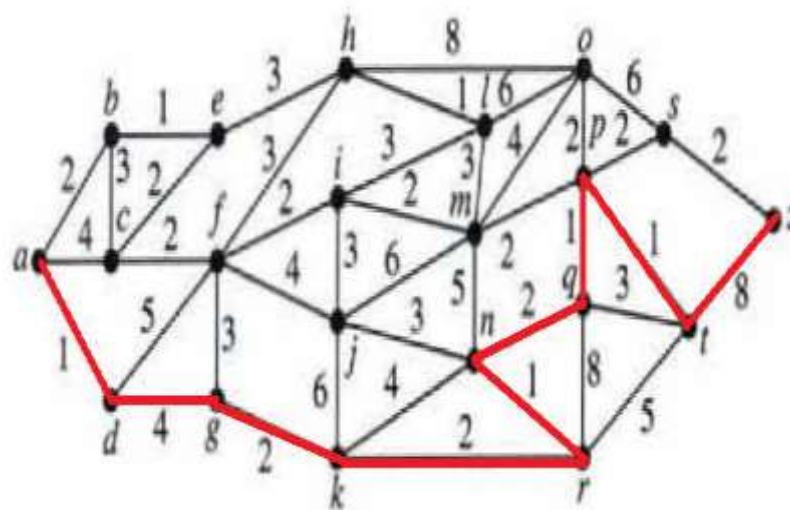


Figure 3.3: Modified Dijkstra Algorithm



Previously

The shortest path Spans A-D-G-K-R-N-Q-T-Z, which is the sum total of these entire path. There we have 22km as the shortest path from A – Z for all vertices reachable from A.

Currently (multiple source and destination vertices application)

(Source)B = E-H-L-M-P=T (Destination) 9

(Source)C = E-H-L-M-P=T (Destination) 11

(Source)D = G-K-R = (Destination) 8

(Source) E =H-L-M-P-T = (Destination) 9

(Source) F =G-K-R-T = (Destination) 12

(Source) G =K-R-T = (Destination) 9

(Source) I =M-P-S= (Destination) 6

(Source) J =N-R-T = (Destination) 9

(Source) K = R-T= (Destination) =7

.

.

. . . . (Destination) S, Z, T

Discussion

The implemented algorithm provides an interactive base in determining multiple shortest hospital paths from various points (town, communities and junction) objectively as opposed to the subjective approach on ground previously. The result was satisfactory having been able to implement multiple source shortest paths as opposed to the single source shortest path sponsored by dijkstra algorithm.

Conclusions

This Paper has demonstrated the practical application of modified Dijkstra algorithm in determining multiple source shortest hospital paths in various hospitals within Rivers State.

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